



# Effect of Cu additions on mechanical properties of $\text{Ni}_3\text{Sn}_4$ -based intermetallic compounds: First-principles calculations and nano-indentation measurements

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## ABSTRACT

The  $(\text{Ni,Cu})_3\text{Sn}_4$  phase as intermetallic compounds (IMCs) plays an important role in evaluating reliability of solder joints. The first-principles calculations were performed to investigate the phase stability, mechanical properties and electronic structures of  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  IMCs. The results shows that the doping of Cu atom not only reduced the phase stability but also weakened the mechanical properties of  $\text{Ni}_3\text{Sn}_4$  crystal structure. Meanwhile, all studied  $\text{Ni}_3\text{Sn}_4$ -based structures were structural stability. Moreover, the anisotropy of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) was strongest while that of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) was the weakest. Based on analysis of electronic structures, it indicated that the ionic bonding of Ni–Cu in  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  structure was weaker than covalent bonding of nearest-neighbor Ni in  $\text{Ni}_3\text{Sn}_4$ , which led to an energy reduction with the formation of banding states. By means of nano-indentation measurements, the young's modulus and hardness were measured to be  $135.3 \pm 8.4$  GPa and  $5.0 \pm 0.63$  GPa for  $\text{Ni}_3\text{Sn}_4$  while  $126.3 \pm 7.6$  GPa and  $4.7 \pm 0.72$  GPa for  $(\text{Ni,Cu})_3\text{Sn}_4$ , respectively, which were close to the value of calculated results.

## 1. Introduction

Soldering is one of the most widely used technologies in electronic package [1–3]. During the progress of soldering, Sn-based solder will melt and react with pad or plated coating to produce intermetallic compounds (IMCs) which connect solder and substrate. However, substantial thickness of IMCs layer will decrease the reliability of solder joints due to the brittleness of IMCs [4]. In recent years, miniaturization is the main trend in the development of electronic packaging produces [5]. As a result, the mechanical properties of IMCs had developed into a key issue in reliability of solder joints and resulted in a great focuses since volume fraction of IMCs became higher with solder joints becoming smaller [6,7]. In fact, the failure behaviors of solder joints are almost controlled by mechanical properties of IMCs [8]. For example, due to the difference of ductility between IMCs layer and substrate, the stress distribution within solder joints will be changed during reflowing and aging, which harms the reliability of electronic packaging produces.

Ni and Ni-based alloys have become common coating materials in ball grid array (BGA) microelectronic packaging while Sn-based solder was used to reflow with Cu substrate, owing to the fact that Ni layer

acted as a barrier layer to impede the diffusion between Sn and Cu element to protect Cu pads. Therefore, the interfacial reactions and IMC growth between Sn-based solders and Ni or Ni-contained substrate have been of interest to many researchers for a long time. Chu et al. [8] researched the interfacial reactions and mechanical reliability of Cu/Sn/Cu and Ni/Sn/Ni sandwich structured solder systems. The results showed that  $\text{Cu}_6\text{Sn}_5$  was formed in the Cu/Sn/Cu system while  $\text{Ni}_3\text{Sn}_4$  was formed in the Ni/Sn/Ni system. Additionally, it also reported that the tensile strength of Ni/Sn/Ni samples was weaker than that of Sn/Cu/Sn samples. Related paper [9] noted that the solder joint reliability and elastic stiffness of IMCs are strong couples. Existing experiment data showed that the Yong's module of  $\text{Ni}_3\text{Sn}_4$  IMC were ranging from 119.4 to 142 GPa [10,11] determined by nano-indentation method. Lee et al. [12] investigated the interfacial reaction of Sn-3.5Ag-0.5Cu (SAC305)/Ni reflowing couples. It reported that  $(\text{Ni,Cu})_3\text{Sn}_4$  was formed between SAC305 solder and Ni pad, and the thickness of IMC layer increased after aging at 150 °C for 2000 h. It has been also observed by other researches that tracts of Cu atoms were often found in the  $\text{Ni}_3\text{Sn}_4$  IMC [13,14], in which Ni sublattice were replaced by Cu atoms. Moreover, solid solubility of Cu element was between 5 and 10 at.% in  $\text{Ni}_3\text{Sn}_4$  phase [15–17]. It is possible that elastic stiffness of

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$\text{Ni}_3\text{Sn}_4$  would be altered with the doping of Cu atom. However, most of researches on  $(\text{Ni,Cu})_3\text{Sn}_4$  IMC were carried out by experimental works and few studies focused on mechanical properties of this IMC. In addition, the influence of the doping of 5–10 at.% Cu atoms on mechanical properties of  $\text{Ni}_3\text{Sn}_4$  IMC is still unknown whether in laboratory or theoretical studies.

This work is aimed to research the effect of Cu additions on mechanical properties of  $\text{Ni}_3\text{Sn}_4$  IMC. The mechanical properties of  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  phases were predicted by means of first-principles calculations. Besides, the systematically works of the phase stability, electronic properties and elastic constants were carried out to understand the difference between the mechanical properties of  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ . Moreover, the  $\text{Ni}_3\text{Sn}_4$  IMCs doped with or without Cu element were produced by reflowing Sn or Sn-0.2Cu solder with Ni substrate. And their Yong's modulus and hardness were measured by using nano-indentation measurements to compare with the predicted results. It is the first systematically work to investigate the mechanical properties of  $(\text{Ni,Cu})_3\text{Sn}_4$  IMC by combining laboratory and theoretical methods.

## 2. Experimental and calculation details

### 2.1. Models and methods

The experimental crystal structure of  $\text{Ni}_3\text{Sn}_4$  [18] was used as the initial model. As shown in Fig. 1(a), the primitive structure of  $\text{Ni}_3\text{Sn}_4$  phase was established, in which Ni atoms occupied two different sites: 2a and 4i sites. Different Ni sites were replaced by Cu atoms according to the formula  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ , in which 7.14 at.% Cu element was doped in the  $\text{Ni}_3\text{Sn}_4$  phase. The solid solubility of Cu element was within the experimental range of 5–10 at.%. Considering the different sites of Ni atoms, two crystal structures of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  IMC were used in this

paper, noted as  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site), which were shown in Fig. 1b and c, respectively.

In this work, the first-principles calculations were carried out with Cambridge serial total energy package (CASTEP) [19]. To ensure the reliability and convergence of calculations, the energy cutoff was set to be 400 eV, and  $3 \times 9 \times 7$  meshes of Monkhorst-Pack k-points were adopted to calculate the lattice parameters and elastic constants ( $C_{ij}$ ) for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  phases. The exchange and correlation functional were treated by the generalized gradient approximation (GGA) for exchange-correlation energy due to Perdew-Burke-Ernzerhof (PBE) [20]. After first-principles calculations, the heat of formation for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  IMCs were calculated by the following formula:

$$\Delta H = E_{\text{total}}(\text{Ni}_x\text{Cu}_y\text{Sn}_z) - [xE_{\text{total}}(\text{Ni}) + yE_{\text{total}}(\text{Cu}) + zE_{\text{total}}(\text{Sn})] \quad (1)$$

in which  $E_{\text{total}}(\text{Ni}_x\text{Cu}_y\text{Sn}_z)$  is the calculated total energy of  $\text{Ni}_x\text{Cu}_y\text{Sn}_z$  at equilibrium lattice constants,  $E_{\text{total}}(\text{Ni})$ ,  $E_{\text{total}}(\text{Cu})$  and  $E_{\text{total}}(\text{Sn})$  are the energy of the isolated Ni, Cu and Sn atoms,  $x$ ,  $y$  and  $z$  are the number of Ni, Cu and Sn atoms in  $\text{Ni}_x\text{Cu}_y\text{Sn}_z$ , respectively. Voight-Reuss-Hill (VRH) approximation [21] was used to obtain the bulk and shear modulus of  $\text{Ni}_3\text{Sn}_4$  and  $(\text{Ni,Cu})_3\text{Sn}_4$  IMCs. The elastic modulus and Poisson's ratio were calculated by the following equations:

$$B = (B_V + B_R)/2 \quad (2)$$

$$G = (G_V + G_R)/2 \quad (3)$$

$$E = 9BG/(3B + G) \quad (4)$$

$$\nu = (3B - 2G)/[2(3B + G)] \quad (5)$$

### 2.2. Experimental works

In the present study,  $\text{Ni}_3\text{Sn}_4$  IMC was produced by soldering Sn ingot with Ni substrate while  $(\text{Ni,Cu})_3\text{Sn}_4$  IMC was produced by soldering Sn-0.2Cu alloy with Ni substrate. The raw materials required for this experiment were pure Sn and pure Cu powder (with 99.99% purity). Fig. 2 [14] shows the phase diagrams of Sn–Cu–Ni alloys. According to the weight percentage of Sn-0.2Cu alloy, the ratio of pure Sn powder and pure Cu powder were put into a vacuum induction melting furnace equipped with a pure argon injection system at 500 °C to produce Sn-0.2Cu solder. During melting, the vacuum atmosphere was necessary to obtain a homogeneous Sn-0.2Cu alloy [22,23]. After the materials were completely melted, the liquid melt was isothermally held at 500 °C for about 3 h. After cooling, the original ingot required

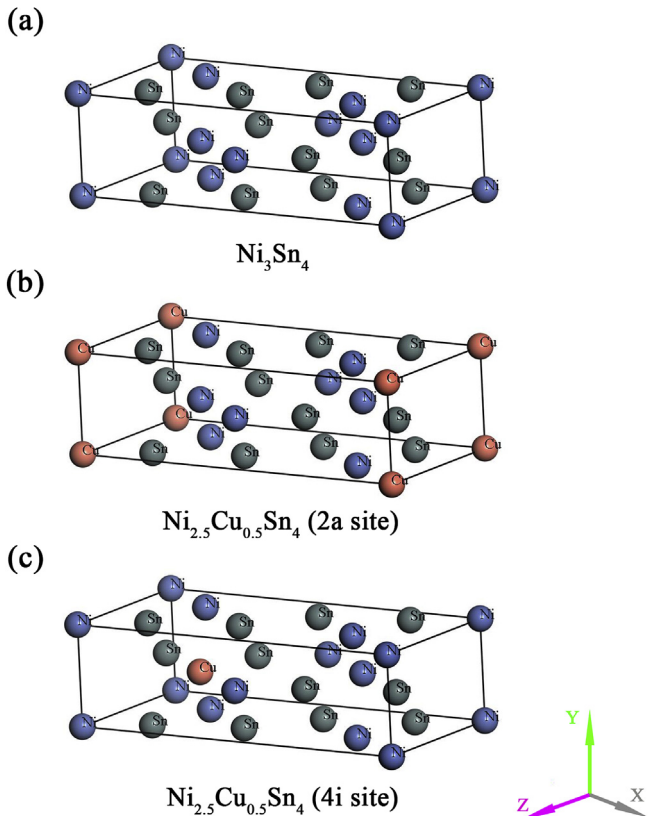


Fig. 1. Crystal structures of (a)  $\text{Ni}_3\text{Sn}_4$ ; (b)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ , in which Cu at 2a site; (c)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ , in which Cu at 4i site.

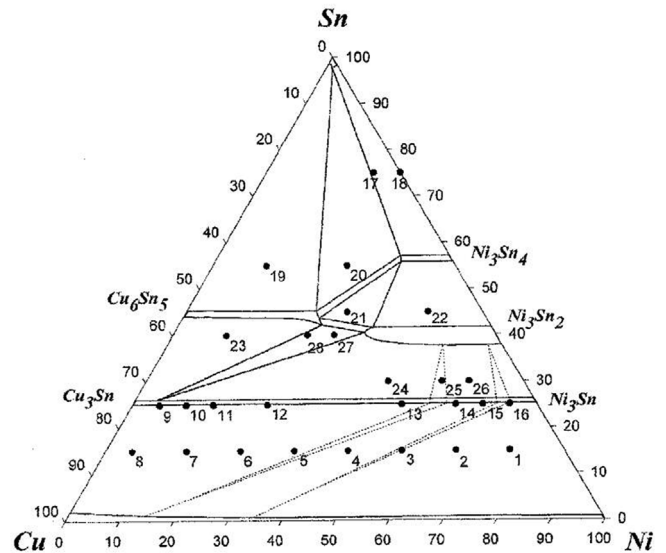


Fig. 2. The phase diagrams of Sn–Cu–Ni alloys [14].

for the experiment was produced.

Ni plates (99.99%) with dimensions  $20 \times 10 \times 2 \text{ mm}^3$  were used as substrates in this work. Before reflowing, the surface of Ni substrates were carefully polished by using  $0.1 \mu\text{m}$  diamond paste, rinsed in water and methanol alcohol and dried. The dip soldering was carried out as following: Firstly, the Sn or Sn-0.2Cu solder was put into a graphite crucible and heated to the temperature of  $230^\circ\text{C}$ . Then, the Ni substrates were carefully immersed in the melted solder for 15 s at the temperature of  $230^\circ\text{C}$  and cooled in air. Finally, the surfaces of the dip soldered joints were cleaned by using methanol alcohol. After dipping soldering, the Sn/Ni and Sn-0.2Cu/Ni couples were aged at  $230^\circ\text{C}$  for 3 h. During the progress of nano-indentation experiments, a thick IMC layer could allow nano-indentation to accurately work and easily neglect the influence of the surrounding softer layers. The selected temperature and time of liquid-state aging ensured that  $\text{Ni}_3\text{Sn}_4$  and  $(\text{Ni,Cu})_3\text{Sn}_4$  IMCs could accumulate to sufficient thickness, which could improve reliability and accuracy of the experimental results. To analyze the elements of IMCs between Sn or Sn-0.2Cu solder and Ni substrate, the scanning electron microscope (SEM, FEI Quanta200F) and energy dispersive X-ray (EDX) were employed. Before metallographic observations, the reflowed samples were mounted in epoxy and then cross-sectioned in a direction perpendicular to the solder/Ni interface. After that, the specimens were carefully polished and etched with a solution containing 3% HCl, 5%  $\text{HNO}_3$  and 92%  $\text{CH}_3\text{OH}$ .

The nano-indentation measurement with a triangular tip was used to measure the Young's modulus and hardness of  $\text{Ni}_3\text{Sn}_4$  and  $(\text{Ni,Cu})_3\text{Sn}_4$ . In this work, the target depth and strain rate were set to be 1000 nm and 0.2 mN/s. As schematically shown in Fig. 3, nano-indentation tests were carried out within the IMC layer between Sn or Sn-0.2Cu solder and Ni substrate. In order to gain reliable data, ten independent experiments were carried out at individual solder joint.

### 3. Results and discussion

#### 3.1. Structure optimization

The lattice constants and the heat of formation for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  obtained from experiments and calculations were summarized in Table 1. It could be found that equilibrium lattice parameters obtained in our theoretical works were agreed with available experimental data [18]. The largest deviation was only 1.84% for lattice constant  $a$  of  $\text{Ni}_3\text{Sn}_4$ , confirming the accuracy of our calculations. It could be observed that Cu in all phases had little influence on lattice constants, which showed that crystal structures were not changed after the doping of Cu atom into  $\text{Ni}_3\text{Sn}_4$  phase. To uncover the effect of Cu additions on phase stability of  $\text{Ni}_3\text{Sn}_4$ , the heat of formation ( $\Delta H$ , meV/atom) at zero temperature and pressure for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  were calculated. A negative value indicates the phase stability with respect to the elemental constituents. Based on our calculations results, all the heat of formation for  $\text{Ni}_3\text{Sn}_4$ -based structures were negative,

**Table 1**

The lattice constants  $a$ ,  $b$  and  $c$  (Å), angle  $\beta$  ( $^\circ$ ) and the heat of formation ( $\Delta H$ , meV/atom) of  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  obtained from experiments and calculations.

Phases	$a$	$b$	$c$	$\beta$	$\Delta H$	Method
$\text{Ni}_3\text{Sn}_4$	12.418	4.111	5.315	105.48	−267	Calculation
	12.214 <sup>a</sup>	4.060 <sup>a</sup>	5.219 <sup>a</sup>	105.50 <sup>a</sup>	−	Experiment
	12.215 <sup>b</sup>	4.060 <sup>b</sup>	5.291 <sup>b</sup>	105.01 <sup>b</sup>	−234 <sup>c</sup>	Calculation
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (2a site)	12.381	4.155	5.330	106.02	−208	Calculation
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (4i site)	12.426	4.101	5.363	105.69	−193	Calculation

<sup>a</sup> Ref. [18].

<sup>b</sup> GGA-PBE calculated results from Ref. [9].

<sup>c</sup> GGA-PBE calculated results from Ref. [24].

implying the stability at zero temperature and pressure. The heat of formation for  $\text{Ni}_3\text{Sn}_4$  was  $-267$  meV/atom, which was close to previous calculation result of  $-234$  meV/atom [24]. When Cu atoms were doped in  $\text{Ni}_3\text{Sn}_4$  structure, the heat of formation increased slightly, with  $\Delta H = -208$  meV/atom for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and  $\Delta H = -193$  meV/atom for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site), which meant that the structure of  $\text{Ni}_3\text{Sn}_4$  was more stable than that of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  IMCs. In other word, the doping of Cu atom weakened the structural stability of  $\text{Ni}_3\text{Sn}_4$  IMC.

#### 3.2. Mechanical properties

In order to study the effect of Cu additions on mechanical properties of  $\text{Ni}_3\text{Sn}_4$  phase, the stiffness elastic constants  $C_{ij}$  (GPa) and compliance elastic constants  $S_{ij}$  (1/GPa) of  $\text{Ni}_3\text{Sn}_4$ -based structures were calculated in this work. The calculated results were listed in Tables 2 and 3. The mechanical stability of crystal structure could be determined by using independent elastic constants. For  $\text{Ni}_3\text{Sn}_4$ -based structures (monoclinic crystal structure), elastic constants should satisfy the following stability criteria [25]:

$$C_{ii} > 0 \quad (i = 1-6), [C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})] > 0$$

$$(C_{33}C_{55} - C_{35}^2) > 0, (C_{44}C_{66} - C_{46}^2) > 0, (C_{33}C_{22} - 2C_{23}^2) > 0. \quad (6)$$

From Table 2, for calculated elastic constants  $C_{ij}$  of all  $\text{Ni}_3\text{Sn}_4$ -based structures, the corresponding criteria listed in Eq. (6) were easily satisfied. Therefore, the studied  $\text{Ni}_3\text{Sn}_4$ -based structures were mechanical stability at 0 K.

The independent elastic constants could be used to derive theoretical elastic modulus by using VRH approach. The calculated results were shown in Table 4. The Young's modulus of  $\text{Ni}_3\text{Sn}_4$  phase was 136.78 GPa, which was consistent with the value of 138 GPa determined by nano-indentation measurements [10]. After Cu doping in  $\text{Ni}_3\text{Sn}_4$  structure, the shear modulus and Young's modulus decreased appreciably, with  $G = 48.18$  GPa and  $E = 123.99$  GPa for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) while  $G = 49.62$  GPa and  $E = 127.45$  GPa for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site). It is predicted that the bonding energy of  $\text{Ni}_3\text{Sn}_4$ -based structures was reduced after doping Cu atoms into  $\text{Ni}_3\text{Sn}_4$  crystal, which led to the decrease of shear modulus and Young's modulus.

According to Pugh's criterion [26], the ratio of  $B/G$  is suggested as a condition to distinct brittle and ductile. If the value is higher than 1.75, the material is ductile, otherwise it is brittle. The ratios of  $B/G$  for  $\text{Ni}_3\text{Sn}_4$ ,  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) were 1.82, 2.01 and 1.95, respectively. Thus all  $\text{Ni}_3\text{Sn}_4$ -based phases could be classified as ductile and  $\text{Ni}_3\text{Sn}_4$  IMC was the most ductile among all studied structures. In addition, Poisson's ratio ( $\nu$ ) can be also considered as a parameter to represent the ductile or brittle behaviors of materials when  $\nu$  is higher or lower than 0.25 [27]. According to Poisson's ratio in Table 4, it was expected that all  $\text{Ni}_3\text{Sn}_4$ -based phases were ductile. However, the elastic modulus of IMCs can be predicted by using first-principle calculations, but the actual plastic properties of materials are

#### Top view

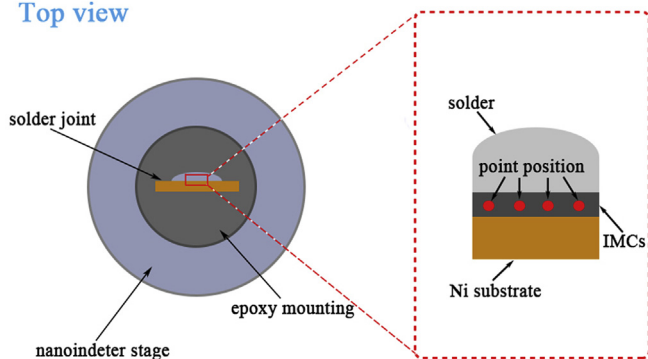


Fig. 3. The locations for nano-indentation tests in tested samples.

**Table 2**The calculated elastic constants  $C_{ij}$  (GPa) for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ .

Phases	$C_{11}$	$C_{12}$	$C_{13}$	$C_{22}$	$C_{23}$	$C_{33}$	$C_{44}$	$C_{55}$	$C_{66}$	$C_{15}$	$C_{25}$	$C_{35}$	$C_{46}$
$\text{Ni}_3\text{Sn}_4$	155.48	70.68	69.34	164.33	68.26	149.86	62.74	59.99	59.95	−21.97	13.99	−8.73	4.90
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (2a site)	139.83	71.74	65.73	154.57	77.70	154.85	60.10	59.68	56.86	−21.33	13.95	−9.57	6.27
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (4i site)	146.95	71.79	64.07	176.30	73.29	154.47	57.86	55.11	55.41	−21.79	11.93	−6.18	8.22

also influenced by crystal structures, microstructures, experimental situations and so on [24]. Ghosh researched the ambient temperature isotropic elastic modulus and plastic properties of  $\text{Ni}_3\text{Sn}_4$  [28]. It is noted that the  $\text{Ni}_3\text{Sn}_4$  exhibited brittle behaviors under Vickers indentation. But few slip bands were also be observed during the experiment, which implied the limited intrinsic ductility of  $\text{Ni}_3\text{Sn}_4$  phase. The results showed that the actual plastic properties of materials were rather complex. The  $\text{Ni}_3\text{Sn}_4$ -based phases were classified as ductile by Pugh's criterion in this work, but the actual experimental responses might deviate from this.

It is generally believed that the mechanical responds of materials are largely influenced by evolution and development of microcracks, which is related to elastic anisotropy [29,30]. The elastic anisotropy of a crystal structure was characterized by the universal elastic anisotropy index ( $A^U$ ) in our work, which could be calculated by the following equation [31]:

$$A^U = 5 \frac{G_V}{G_R} + \frac{B_V}{B_R} - 6 \geq 0 \quad (7)$$

in which  $G_V$ ,  $G_R$ ,  $B_V$  and  $B_R$  represented the shear modulus and bulk modulus calculated by Voight and Reuss methods, respectively. When the value of  $A^U$  is zero, the crystal structure should be an isotropic structure. A larger value of  $A^U$  reveals a stronger anisotropy for a material. The calculated results were listed in Table 5. According to Table 5, all  $\text{Ni}_3\text{Sn}_4$ -based crystal structures were not isotropic structure. Meanwhile, the Cu doping would strengthen the mechanical anisotropy of  $\text{Ni}_3\text{Sn}_4$  IMC only at a special occupancy site (2a site). In order to further illustrate the mechanical anisotropy of  $\text{Ni}_3\text{Sn}_4$ -based phases, curved surfaces of three-dimensional (3D) were employed in this work. The surface constructions of Young's modulus were defined in the following equation:

$$E^{-1} = l_1^4 S_{11} + 2l_1^2 l_2^2 S_{12} + 2l_1^2 l_3^2 S_{13} + 2l_1^2 l_5^2 S_{15} + 2l_2^4 S_{22} + 2l_2^2 l_3^2 S_{23} + 2l_1 l_2^2 l_3 S_{25} + l_3^4 S_{33} + 2l_1 l_3^3 S_{35} + l_2^2 l_3^2 S_{44} + 2l_1 l_2^2 l_3 S_{46} + l_1^2 l_3^2 S_{55} + l_1^2 l_2^2 S_{66}. \quad (8)$$

Here  $l_1$ ,  $l_2$  and  $l_3$  represented the direction cosines to the x, y and z axes, respectively.  $S_{ij}$  were calculated to be elastic constants, as shown in Table 3. The surface construction of an isotropic crystal exhibited to be spherical, while the degree deviating from sphere implied the content of anisotropy. As shown in Fig. 4, the  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) had the strongest anisotropy while the  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) had the weakest one. Related paper showed that the elastic modulus of  $\text{Ni}_3\text{Sn}_4$  IMC varied over a wide range. For example, the reported Young's modulus of  $\text{Ni}_3\text{Sn}_4$  phase ranged from 119 to 152 GPa determined by nano-indentation measurements [11,12,32] while between 94 and 118 GPa determined by other methods [10,28]. The analysis of elastic anisotropy made it easy to understand the wide range of elastic modulus of  $\text{Ni}_3\text{Sn}_4$ .

**Table 3**The calculated elastic constants  $S_{ij}$  (1/GPa) for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ .

Phases	$S_{11}$	$S_{12}$	$S_{13}$	$S_{22}$	$S_{23}$	$S_{33}$	$S_{44}$	$S_{55}$	$S_{66}$	$S_{15}$	$S_{25}$	$S_{35}$	$S_{46}$
$\text{Ni}_3\text{Sn}_4$	0.0098	−0.0034	−0.0027	0.0090	−0.0027	0.0092	0.0160	0.0191	0.0168	0.0030	−0.037	0.0010	−0.0013
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (2a site)	0.0112	−0.0045	−0.0022	0.0110	−0.0039	0.0094	0.0166	0.0198	0.0178	0.0047	−0.0048	0.0016	−0.0018
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (4i site)	0.0102	−0.0035	−0.0024	0.0084	−0.0027	0.0088	0.0177	0.0208	0.0184	0.0045	−0.0035	−0.0006	−0.0026

**Table 4**The calculated bulk modulus ( $B$ , GPa), shear modulus ( $G$ , GPa), Young's modulus ( $E$ , GPa) and Poisson's ratio ( $\nu$ ) for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ .

IMCs	$B$	$G$	$E$	$\nu$	$B/G$
$\text{Ni}_3\text{Sn}_4$	98.01	53.96	136.78	0.270	1.82
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (2a site)	96.88	48.18	123.99	0.287	2.01
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (4i site)	98.45	49.62	127.45	0.284	1.95

**Table 5**The calculated bulk modulus (GPa) and shear modulus (GPa) in VRH approximations and the universal anisotropy index ( $A^U$ ) for  $\text{Ni}_3\text{Sn}_4$ -based structures.

IMCs	$B_V$	$B_R$	$G_V$	$G_R$	$B_V/B_R$	$G_V/G_R$	$A^U$
$\text{Ni}_3\text{Sn}_4$	98.47	97.56	53.96	49.42	1.001	1.092	0.461
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (2a site)	97.73	96.03	51.11	45.25	1.018	1.130	0.668
$\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ (4i site)	99.56	97.33	51.58	47.66	1.013	1.082	0.423

### 3.3. Electronic structures

To gain deep insight into the nature of the electronic structures, the calculated total density of states (DOS) and partial density of states (PDOS) were shown in Fig. 5, in which Fermi level ( $E_F$ ) was located at 0 eV and marked by the dashed line. In all cases, it was a remarkable fact that several bands crossed the Fermi level. The electronic property showed that the  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  phases were metallic. For  $\text{Ni}_3\text{Sn}_4$ , the sum DOS at energy range from about −12 to −6 eV was main contributed by Sn-s state. In the zone from about −6 eV to  $E_F$ , the Ni-d state was the dominant part of the sum DOS while the Sn-p state made significant contributions to DOS. Within the energy range from  $E_F$  to −6 eV, the sum DOS was mainly contributed by Ni-d and Sn-p states. The results were in good agreement with the results of Ghosh [33].

According to a direct comparison between the sum DOS of Cu-doped and Cu-free  $\text{Ni}_3\text{Sn}_4$ -based structures, it was clear to find that the bonding peak between −3 and −1 eV was main difference and the lower bonding peak appeared in both  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) phases. It was contributed to that when Ni sites were replaced by Cu atoms in  $\text{Ni}_3\text{Sn}_4$  structure, the amplitude of the Ni-d state peak was significantly reduced by the reason of the low Ni concentration in  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  phases, which weakened the bonding between Ni and Sn atoms. Another difference between the DOS of  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  phases was that a second bonding peak appeared at the energy ranging from −5 to −3 eV in Cu-doped structures, which was ascribed to the contribution of Cu-d state. However, the peak position of Cu-d state corresponded to the saddle-point position of Sn-p at the energy level of about −4.5 eV, thus the doped Cu atoms were not able to accommodate the loss of the bonding between Ni and Sn. In a word, the bonding energy of  $\text{Ni}_3\text{Sn}_4$  was stronger than that of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  crystal structures. As known, larger bonding energy



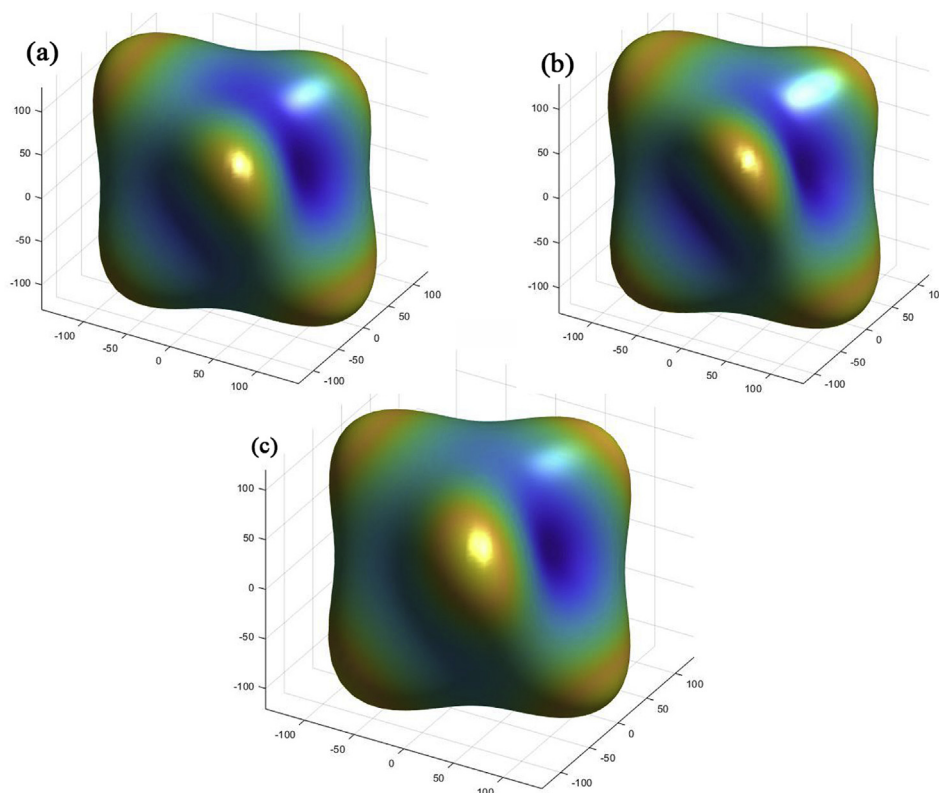


Fig. 4. The surface constructions of Young's modulus for (a)  $\text{Ni}_3\text{Sn}_4$ , (b)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and (c)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site).

correspond to a stronger charge interaction [34], and the structural stability will increase. The results might be the reason for the difference of thermodynamic stability and elastic properties between  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$ .

To further understand the bonding mechanisms in  $\text{Ni}_3\text{Sn}_4$ -based structures, the difference charge density maps were illustrated in Fig. 6. The calculated results made it easy to understand the effect of Cu additions on nature of bonding in  $\text{Ni}_3\text{Sn}_4$ -based IMCs. According to Fig. 6(a) and (c), the difference charge density distributions were clearly observed to be positive values at locations of Ni atoms, implying covalent bonding between nearest-neighbor Ni atoms in  $\text{Ni}_3\text{Sn}_4$  crystal structure. When Cu atoms substituted for Ni atoms at 2a sites in  $\text{Ni}_3\text{Sn}_4$  crystal structure, the difference charge density maps were altered significantly. As shown in Fig. 6(b), the difference charge density distributions for sites of Cu atoms were calculated to be negative values, which indicated that ionic bonding was formed between nearest-neighbor Ni and Cu atoms. As shown in Fig. 6(d), when Cu atoms occupied 4i sites of Sn atoms in  $\text{Ni}_3\text{Sn}_4$  crystal structure, the similar effect of additional Cu on nature of bonding in  $\text{Ni}_3\text{Sn}_4$ -based IMCs was discovered, in which the previous Ni–Ni covalent bonding in Cu-free phase changed to be Cu–Ni ionic bonding in Cu-doped phase. As well known, the banding strength of covalent bonding is greater than that of ionic bonding. Therefore, when Cu atoms were doped in  $\text{Ni}_3\text{Sn}_4$  phase, it indicated that the ionic bonding of the nearest-neighbor Ni and Cu atoms was weaker than the previous Ni–Ni covalent bonding, which led to an energy reduction with the formation of banding states. The results showed that  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  IMCs were less resistant to deformation than  $\text{Ni}_3\text{Sn}_4$ , which could explain the mechanism of the decrease of stability and modulus of  $\text{Ni}_3\text{Sn}_4$ -based structures.

### 3.4. Experimental results

The typical cross-section microstructures of solder joints were shown in Fig. 7. In order to confirm the crystal structures of interfacial

IMCs between solder and substrate, the EDX and XRD were used in this work. The EDX and XRD results were well presented in Figs. 8 and 9, respectively. For each samples, several analyses were adopted to ensure the reliable of tests. XRD analyses showed that  $\text{Ni}_3\text{Sn}_4$  structure was identified in Sn/Ni reaction couples. EDX results of the IMC particles showed that  $\text{Ni}_3\text{Sn}_4$  phase was composed of 41.38 at.% Ni and 58.62 at.% Sn. For the interfacial IMC formed between Sn-0.2Cu solder and Ni substrate, structural analyses showed that the IMC structure was seem to be  $\text{Ni}_3\text{Sn}_4$  structure. EDX results showed that it was composed of 36.44 at.% Ni, 6.93 at.% Cu and 56.63 at.% Sn, which could be confirmed as  $(\text{Ni,Cu})_3\text{Sn}_4$  phase. It meant that Cu element showed minimal solubility in Sn-rich phases, which diffused into  $\text{Ni}_3\text{Sn}_4$  to produce  $(\text{Ni,Cu})_3\text{Sn}_4$ . The results were well agreed with the previous researches [15,16]. It also observed from Fig. 7 that the average thickness of IMC layer accumulated to 34.36  $\mu\text{m}$  for  $\text{Ni}_3\text{Sn}_4$  and 21.79  $\mu\text{m}$  for  $(\text{Ni,Cu})_3\text{Sn}_4$  during soldering and liquid-state aging, which allowed easy nano-indentation works while safely neglected the influence of the surrounding softer layers. The location and shape of nanoindentations at the solder joint surface were shown and marked by square regions in Fig. 7. It suggested that the target depth and strain rate adopted during nano-indentation experiments were reasonable to measure a single IMC layer and thus the results obtained in this work were reliable and valuable.

In order to discover the effect of additional Cu atoms on the mechanical properties of interfacial IMCs with solder joints, nano-indentation measurements were carried out in this work. Fig. 10 shows the representative indentation loading-depth curves of  $\text{Ni}_3\text{Sn}_4$  and  $(\text{Ni,Cu})_3\text{Sn}_4$  IMCs with 0.2 mN/s strain rate at the maximum depth of 1000 nm. It was clearly observe that under the same experimental conditions, the required load for  $(\text{Ni,Cu})_3\text{Sn}_4$  IMC was lower than  $\text{Ni}_3\text{Sn}_4$  IMC to reach the maximum depth of 1000 nm. It indicated that the mechanical properties of  $\text{Ni}_3\text{Sn}_4$  phase were weakened with the doping of Cu atoms, which agreed well with experiment results. For  $\text{Ni}_3\text{Sn}_4$  IMC, the obtained average values of Young's modulus and hardness were  $135.3 \pm 8.4$  GPa and  $5.0 \pm 0.63$  GPa, respectively,

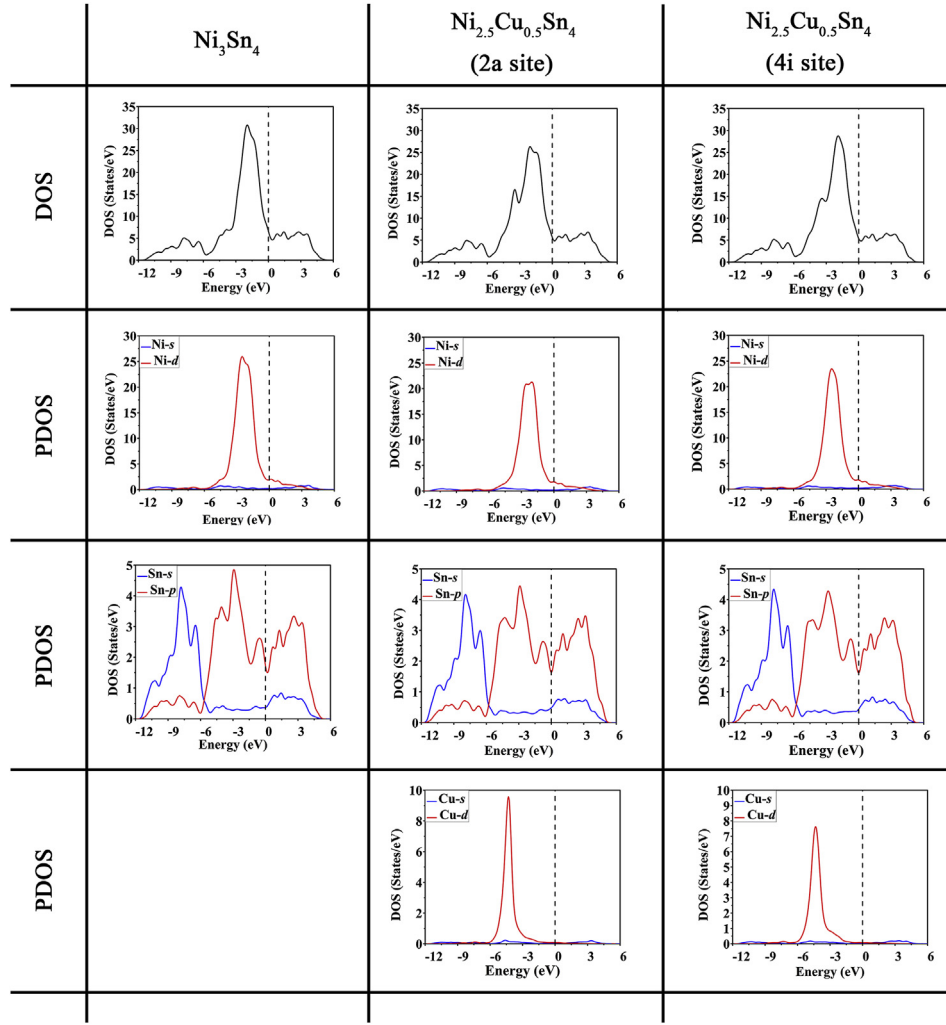


Fig. 5. Density of states (DOS) for  $\text{Ni}_3\text{Sn}_4$  and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  with the partial density of states (PDOS) for Ni, Sn and Cu atoms.

which were close to previous results [11,32], in which  $E = 134.0$  GPa and  $H = 4.8$  GPa. As expected, for  $(\text{Ni,Cu})_3\text{Sn}_4$ , the Young's modulus and hardness were measured to be lower values of  $126.3 \pm 7.6$  GPa and  $4.7 \pm 0.72$  GPa, respectively. It was necessary to point out that Young's modulus of  $\text{Ni}_3\text{Sn}_4$ ,  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) were estimated to be 136.78, 123.99 and 127.45 GPa by following first-principles calculations, respectively, which fell nicely within the ranges of the nano-indentation measurement results. Hence, by combining the results of first-principles calculations and experimental works, it demonstrated that the doping of Cu atom was believed to weaken the mechanical properties of  $\text{Ni}_3\text{Sn}_4$ , which was expected to

provide valuable information for innovation and usage of solder joints.

#### 4. Conclusions

In this work, the first-principles and nano-indentation measurements were employed to research the effect of additional Cu atoms on the crystal structures and mechanical properties of  $\text{Ni}_3\text{Sn}_4$  IMC, and the electronic structures of  $\text{Ni}_3\text{Sn}_4$ -based crystals were also discussed. Our systematical works of first-principles calculations predicted that the doping of Cu atom weakened the mechanical properties of  $\text{Ni}_3\text{Sn}_4$  phase, in which Young's modulus were 136.78 GPa for  $\text{Ni}_3\text{Sn}_4$  while

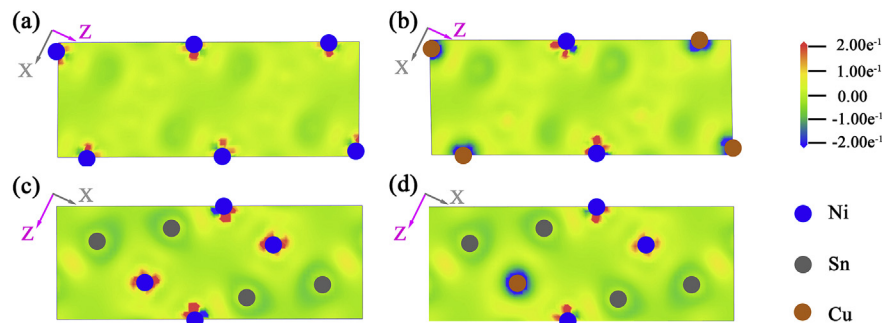


Fig. 6. The difference charge density maps for (a)  $\text{Ni}_3\text{Sn}_4$  in (110) plane, (b)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) in (110) plane, (c)  $\text{Ni}_3\text{Sn}_4$  in (010) plane and (d)  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) in (010) plane.

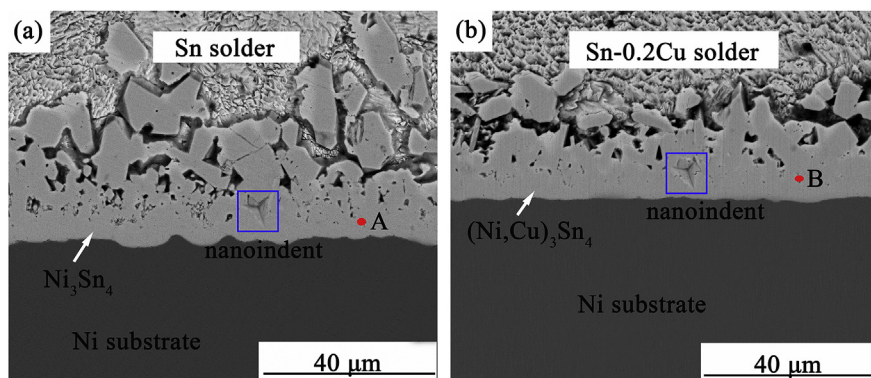


Fig. 7. Cross-sectional microstructure of (a) Sn/Ni reaction couples and (b) Sn-0.2Cu/Ni reaction couples.

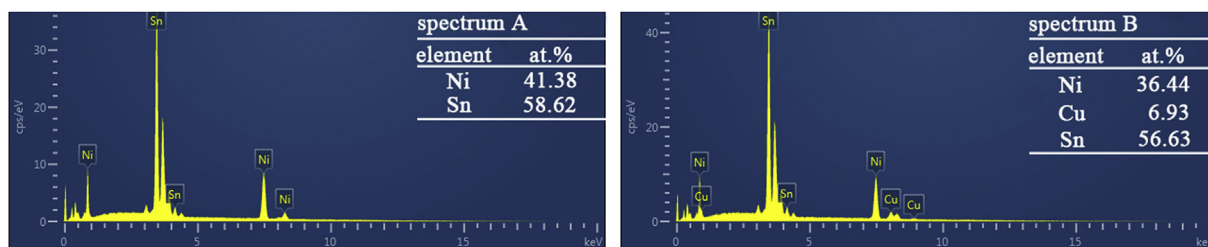


Fig. 8. EDX results of spectra marked in Fig. 7: spectrum A in Fig. 7(a) and spectrum B in Fig. 7(b).

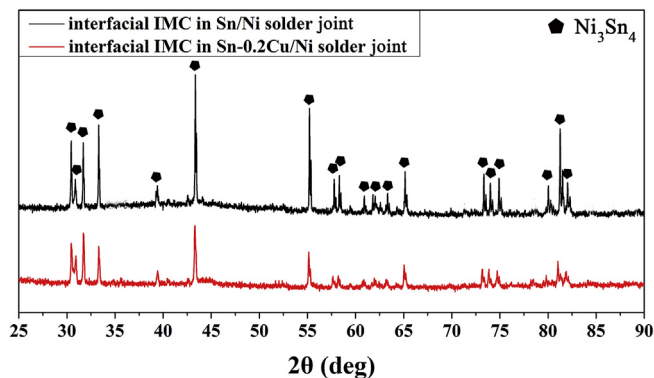


Fig. 9. XRD results for interfacial IMCs of solder joints.

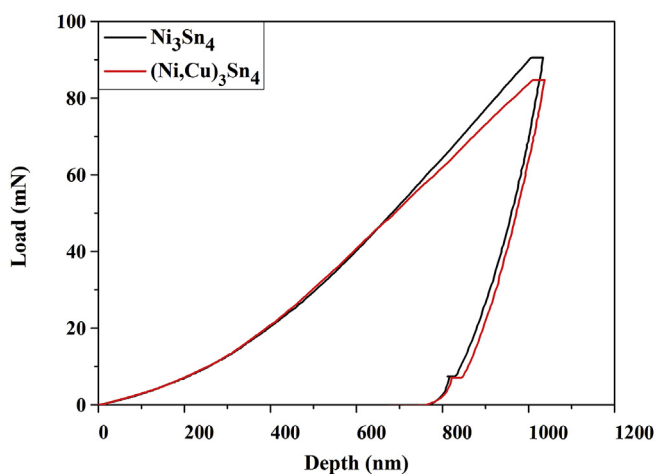


Fig. 10. Indentation loading-depth curves of  $\text{Ni}_3\text{Sn}_4$  and  $(\text{Ni,Cu})_3\text{Sn}_4$ .

123.99 GPa for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) and 127.45 GPa for  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site), respectively. Furthermore, the anisotropy of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (2a site) was the strongest while that of  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  (4i site) was the weakest. Based on the analysis of electronic structures, it indicated that bonding energy between Ni and Sn atoms weakened after the doping of Cu atom, which led to the decrease of Young's modulus. According to the difference charge density maps, the ionic bonding of Ni–Cu in  $\text{Ni}_{2.5}\text{Cu}_{0.5}\text{Sn}_4$  structure was weaker than covalent bonding of nearest-neighbor Ni in  $\text{Ni}_3\text{Sn}_4$ . Our nano-indentation measurements showed that the young's modulus and hardness were  $135.3 \pm 8.4$  GPa and  $5.0 \pm 0.63$  GPa for  $\text{Ni}_3\text{Sn}_4$  while  $126.3 \pm 7.6$  GPa and  $4.7 \pm 0.72$  GPa for  $(\text{Ni,Cu})_3\text{Sn}_4$ , respectively. The calculated Young's modulus fell nicely within the ranges of the experimental results. By combining experimental and calculated results, it was concluded that the doped Cu atoms weakened the mechanical properties of  $\text{Ni}_3\text{Sn}_4$ -based IMCs.

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